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# **Chaos of charged particle orbit in a compact levitated dipole experiment**

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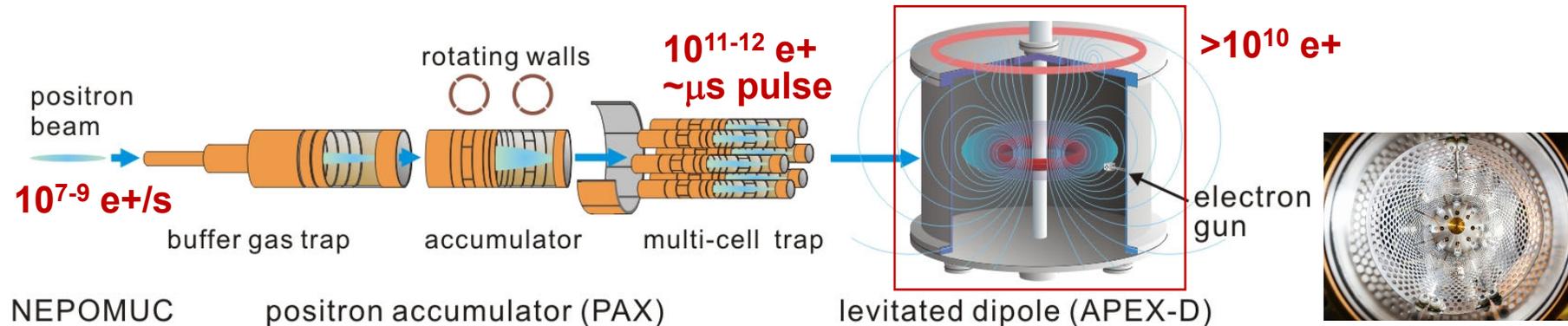
# Outline

- Plan and status of Compact Levitated Dipole for electron-positron pair plasmas
- Motivation to study chaotic orbit of positrons ( $e^+$ s) in CLD
- Mechanism of chaotic orbit in dipole by  $\mu$ - $J$  coupling (high-energy  $e^+$ s in RT-1) ( $> \sim 100$ keV, not straightforward to be conducted in trap experiments)
- Analysis of **chaotic orbit of  $e^+/e^-$ s** in the planned **compact dipole**
  - possibility of chaos with low energy ( $\sim 10$ eV)  $e^+/e^-$
  - condition for the  $\mu$ - $J$  coupling chaotic orbit with low energy particles
  - long flight time of positrons/electrons
- Summary and future work

# Background : Compact levitated dipole towards the formation of electron-positron plasma in laboratory

- Creation of electron-positron plasmas

2020 Higaki+ Appl. Phys. Exp. @AIST/Hiroshima  
2015 Saitoh+ New J. Phys. @NEPOMUC/IPP/TUM



- unique wave/stabilities as pair-plasmas
- astrophysically equivalent experiment

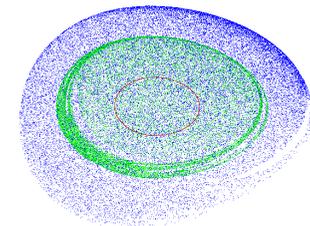


Reactor (FRM-II) based  $e^+$  source

2012 Hugenschmidt+, New J. Phys.

- Application of chaotic orbit in levitated dipole

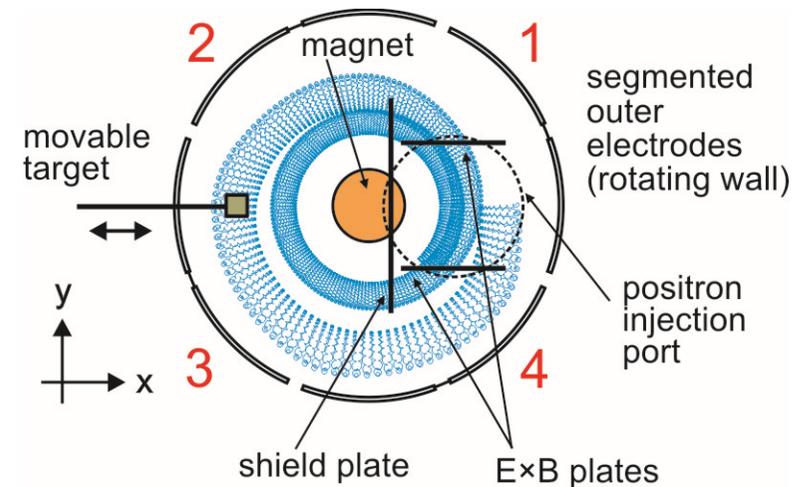
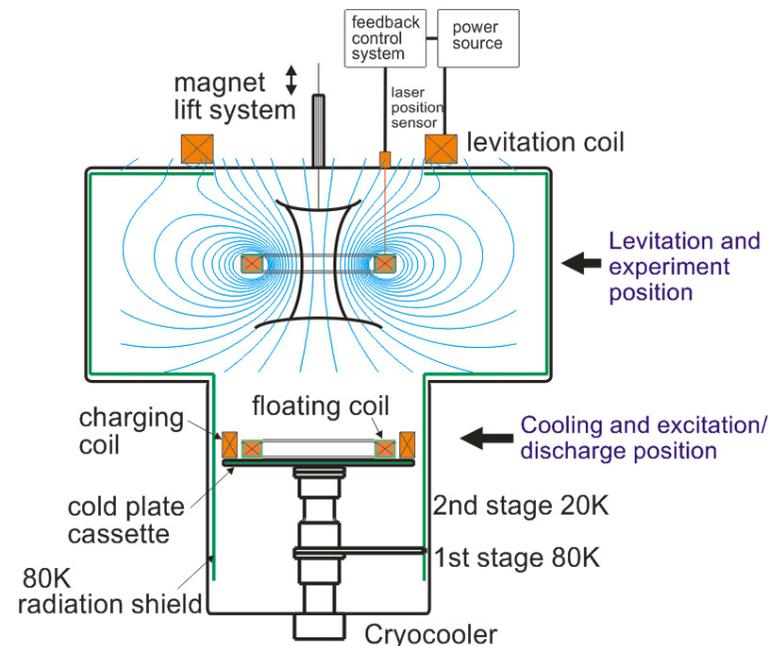
- chaos-induced transport
- injection scheme (long orbit)
- particle mixing (of  $e^+/e^-$  in trap)



With slow positrons, precise measurements are realized with annihilation  $511\text{keV}$   $\gamma$ -rays

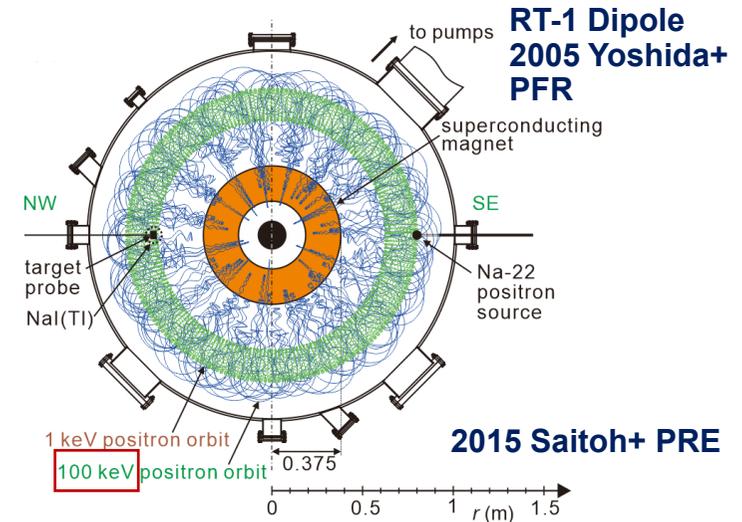
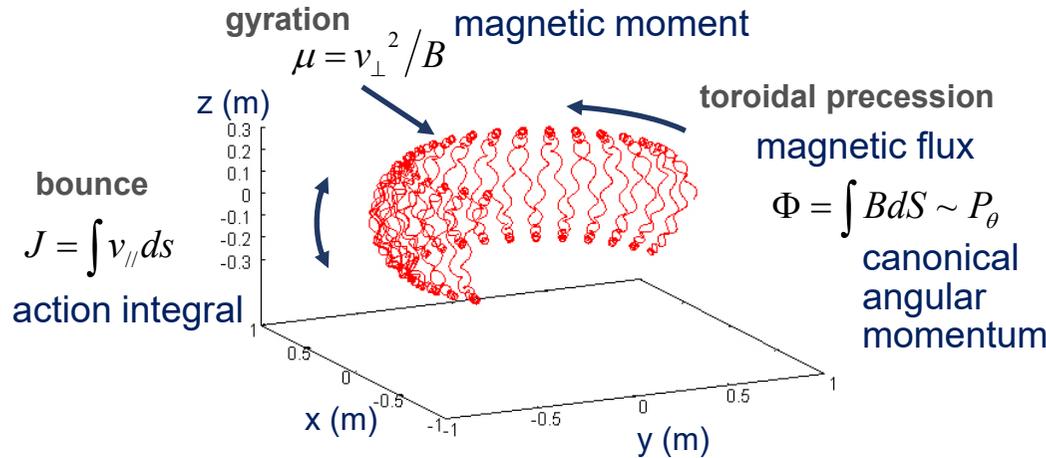
# Motivation to use the properties of chaotic orbit in a compact levitated dipole with low energy particles

- Chaos in an axymmetric dipole field, interesting as its own right
- Toward the efficient injection scheme in a toroidal geometry:
  - For continuous injection, application of rotating wall (RW) is planned in dipole field configuration, which needs several toroidal rotations of particles
  - Chaos may realize long orbit needed for the compression phase with RW



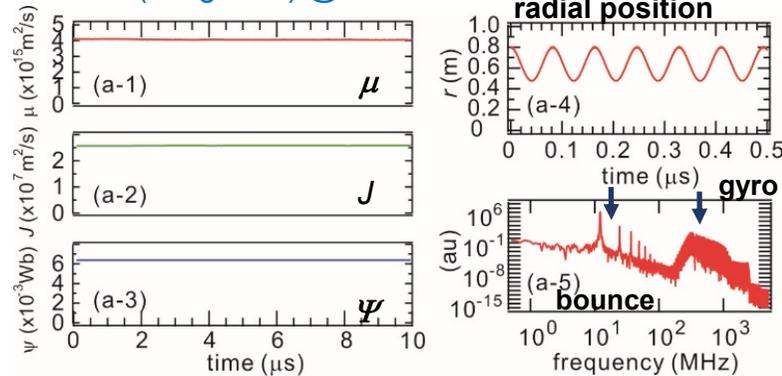
# Mechanism of non-integrable chaotic motion in a dipole field: coupling of gyro and bounce motions

- Three adiabatic invariants (actions for associate periodic motions) + Energy

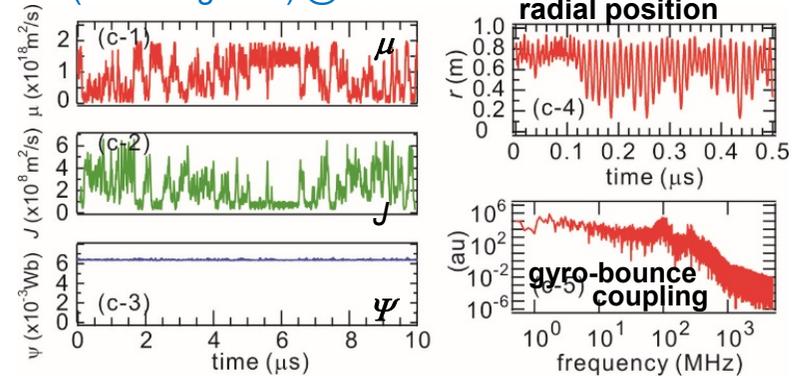


- Only two invariants ( $\Psi$  and  $K$ , not  $\mu$  and  $J$ ) < 3 are conserved

Periodic (integrable) @1keV e+



Chaotic (non-integrable) @100keV e+



coupling of  $\mu$  and  $J$

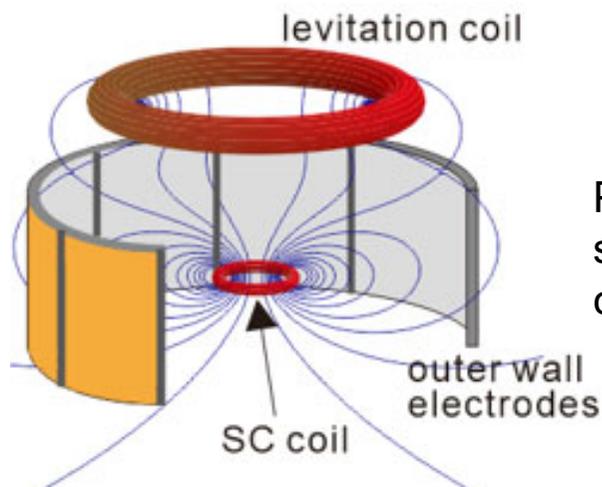
- Such chaotic motion was realized and investigated in RT-1, but **for >100keV e+s**  
**Chaos of low energy e+/e- in a compact levitated dipole (small B, x-point)?**

# Purpose of this study and definition of calculation geometry/conditions

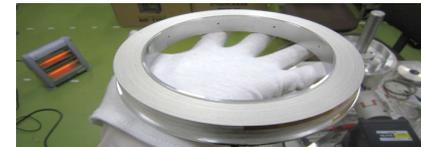
We numerically evaluate the chaos condition in the planed device parameters

Chaotic orbit exists? if so, conditions and effects to extend orbit length?

- We focus on the **coupling of  $\mu$  and  $J$**  (not the breakdown of conservation of  $\Psi$ ): resonance between gyro and bounce motions makes chaos.
- In compact levitated dipole configuration,
  - relatively weak field strength
  - magnetic null near the trap region
 may enhance the chaotic behavior.



Pure dipole and separatrix configuration



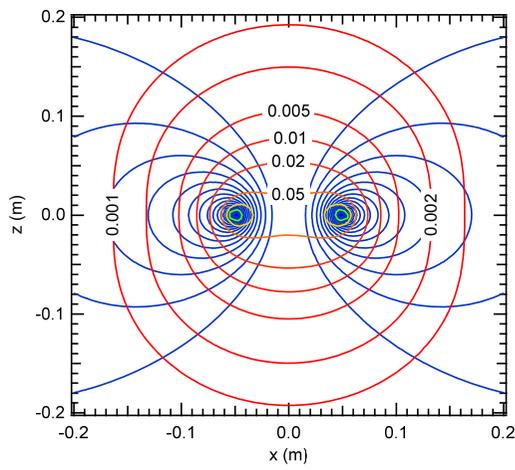
**$2r=10\text{cm}$ , 300 turns HTS (Bi-2223) winding, up to 12kAT (40A/turn)**



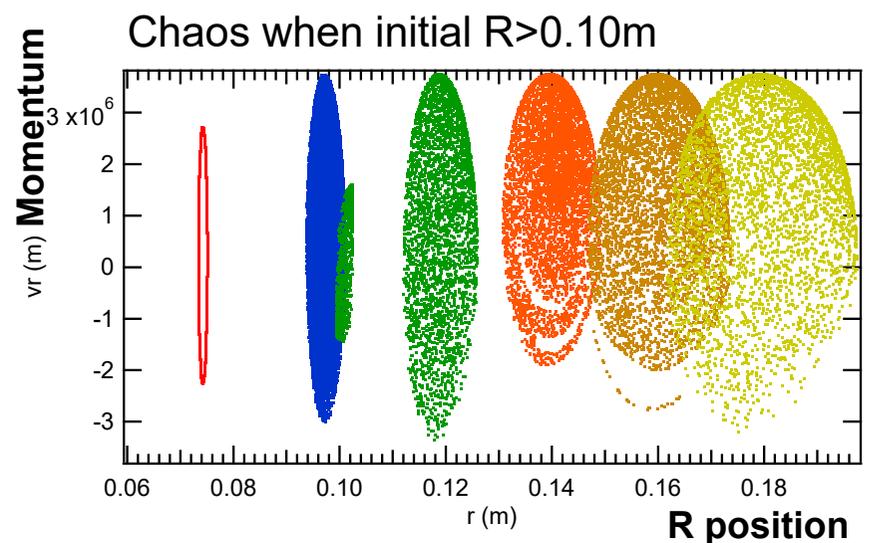
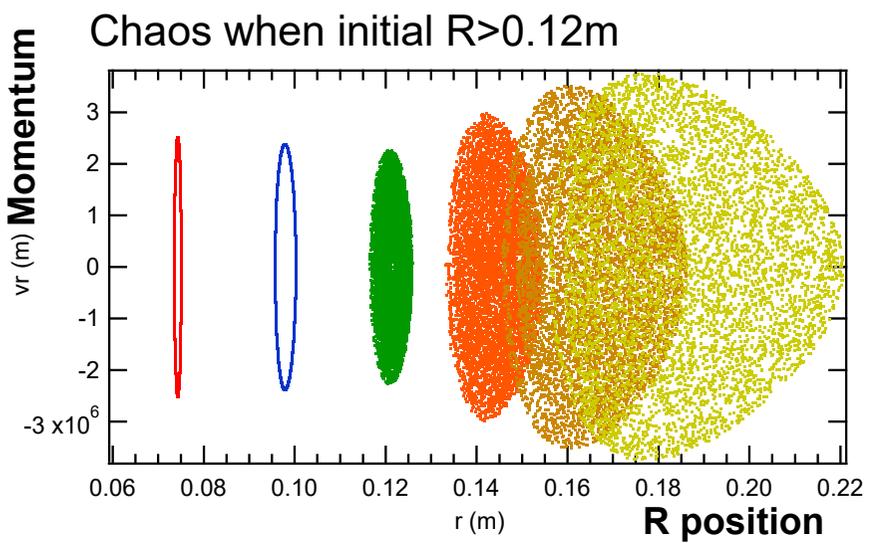
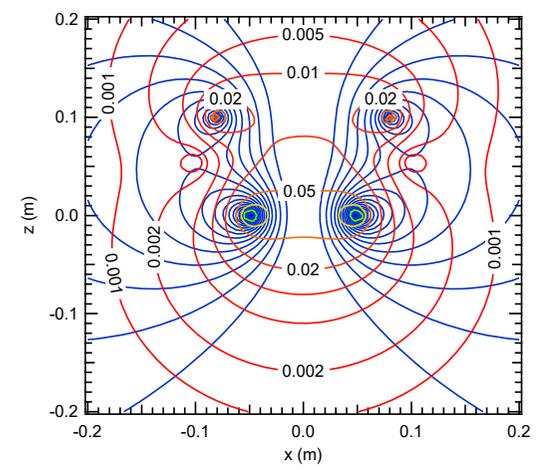
**Feasible with SC charging coil**

# Poincaré plot of orbit shows emergence of chaos even for low energy e<sup>+</sup>/e<sup>-</sup> (K<sub>para</sub> = K<sub>perp</sub> = 10eV)

- Pure dipole config.



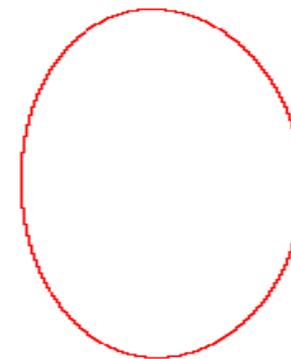
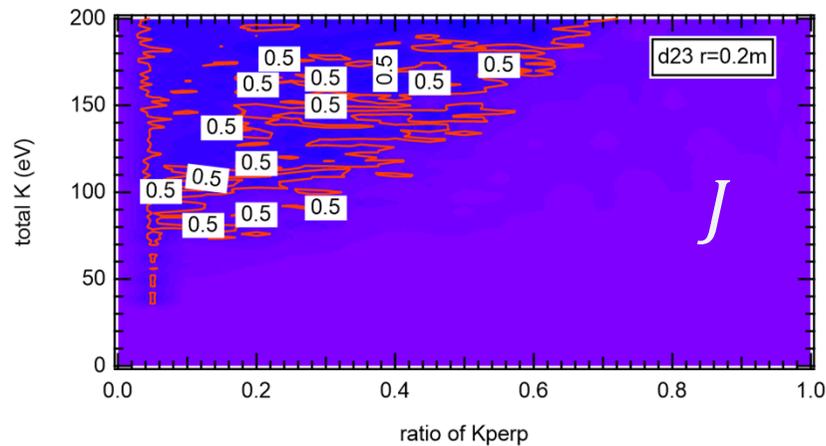
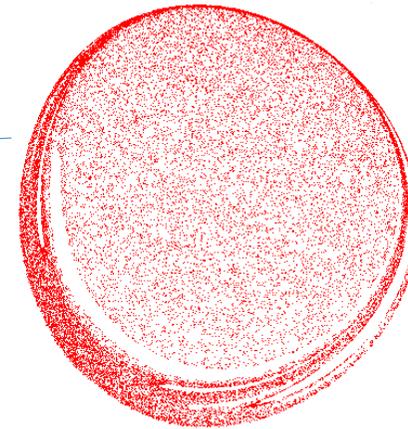
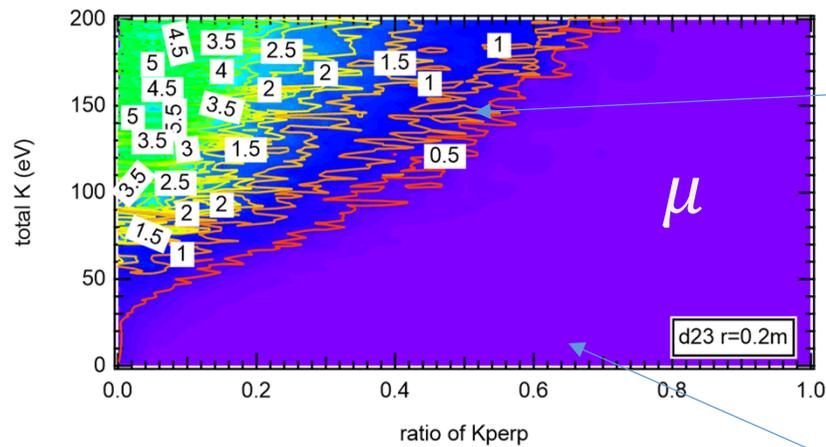
- Separatrix (dipole + levitation coil) config.



20eV positrons take chaotic orbit according to initial radial positions

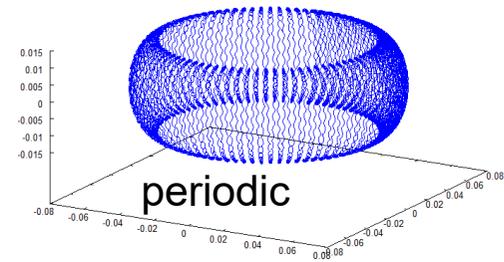
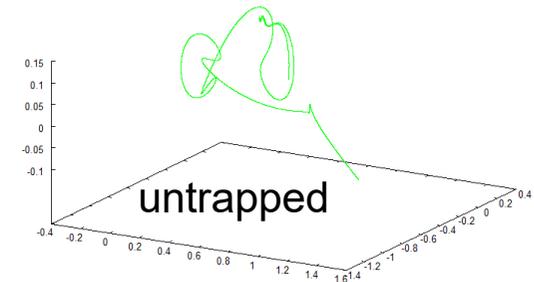
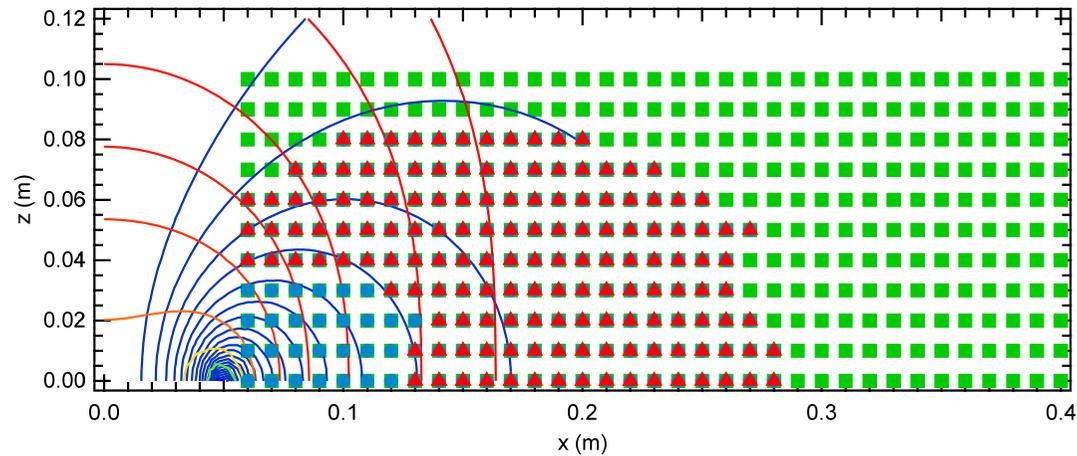
# Simultaneous breakdown of $\mu$ and $J$ conservations

- Simultaneous breakdown of  $\mu$  and  $J$ , indicating the gyro and bounce coupling
- Poincaré plot shows stochastic motion when  $\mu$  and  $J$  are not conserved

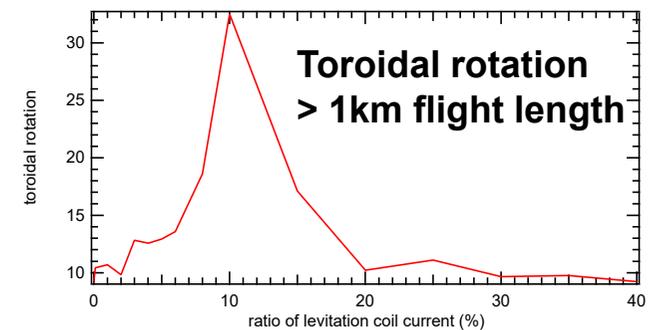
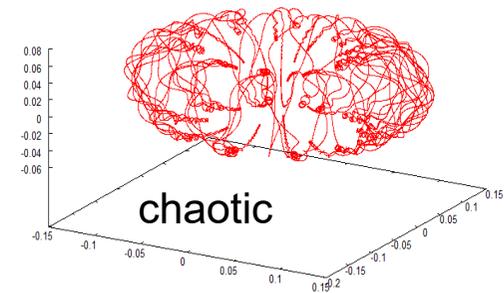
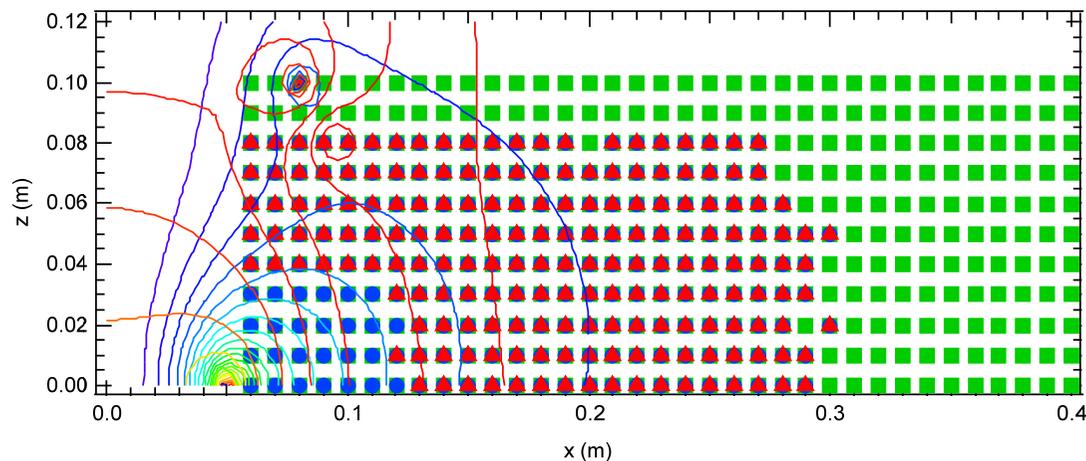


# Broad "chaotic orbit region" exists between regular and untrapped orbit regions

- **Pure dipole config.**



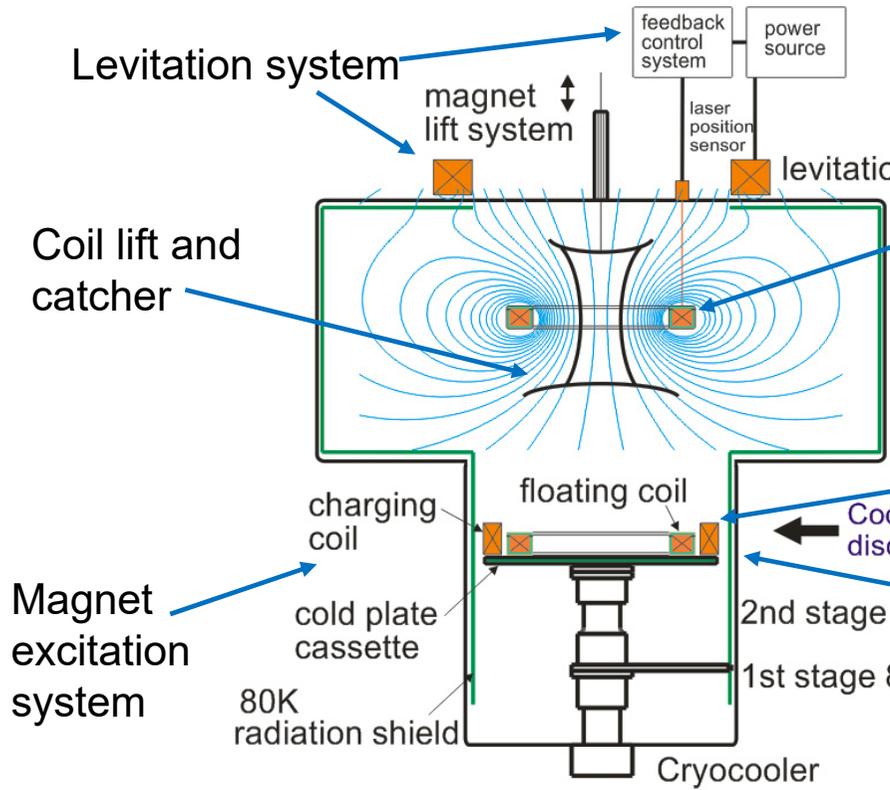
- **Separatrix (dipole + levitation coil) config.**



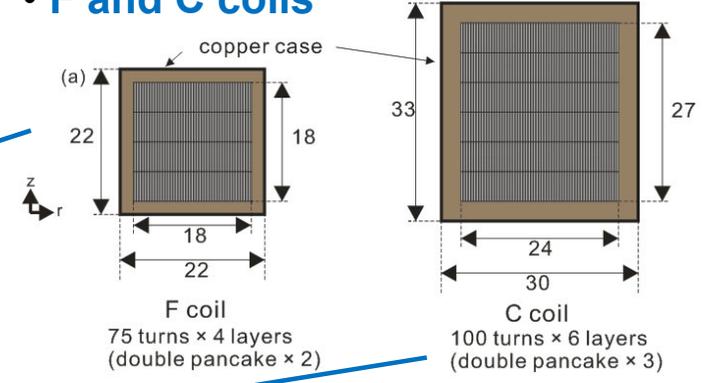
## Summary

- We numerically traced orbit of low energy positrons in a planned compact levitated dipole to investigate conditions for chaotic orbit
- In marked contrast to the case of RT-1 with strong magnetic field, chaotic orbit of low energy ( $\sim 10$  eV) do exist in this geometry
- **Coupling and simultaneous breakdown of  $\mu$  and  $J$**  was identified as mechanism of chaos (only 2 invariants, non-integrable system)
- Dipole trap has a spatially broad "chaotic orbit region" between regular motion and untrapped region
- Positrons/electrons with chaotic orbit have long orbit length ( $\sim$ km) even with mechanical structure of the trap system, which can be useful for the applied for rotating wall E field for orbit compression

# Development of a compact dipole in Japan

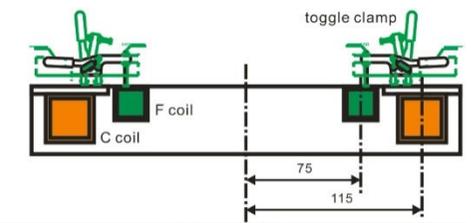


## F and C coils

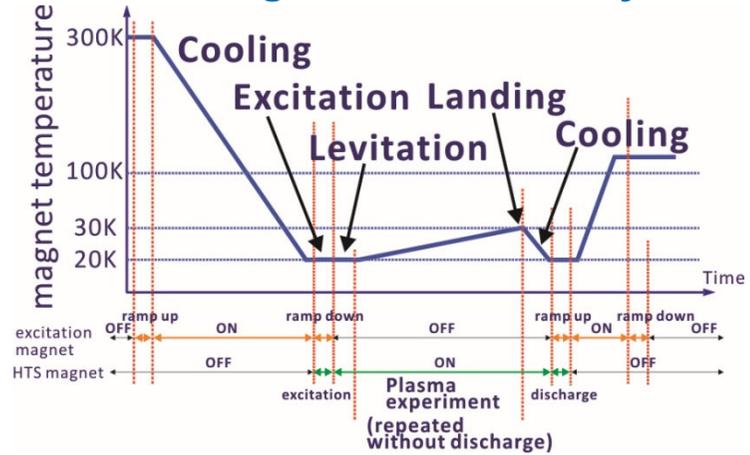


Levitation and experiment position

Cooling and excitation/discharge position



## coil cooling and excitation cycle



## cooling station for the F and C coils

thermal contact of the F coil is realized with toggle clamps

